

1. If $y = \frac{\sin^2 x}{1 + \cot x} + \frac{\cos^2 x}{1 + \tan x}$ then $\frac{dy}{dx}$ at $x = \frac{\pi}{4}$ is
- 0
 - 1
 - 1
 - 2
2. The value of $\cot\left(\frac{1}{2}(3\pi - \tan^{-1}(\frac{1}{3}))\right)$ equals
- $(10 + \sqrt{3})^{-1}$
 - $(3 + \sqrt{10})^{-1}$
 - $(3 + \sqrt{10})$
 - $(10 + \sqrt{3})$
3. $\lim_{x \rightarrow -1^+} \frac{\sin^{-1}(\sqrt{\pi} - \sqrt{\cos^{-1}x})}{\sqrt{1-x^2}}$ equals
- 0
 - 1
 - $\frac{1}{2\sqrt{\pi}}$
 - $\frac{1}{\sqrt{\pi}}$
4. If $f(x) = 3 + (1 + 7^{\frac{1}{1-x}})^{-1}$ then
- $\lim_{x \rightarrow 1^-} f(x) = 4$
 - $\lim_{x \rightarrow 1^+} f(x) = 3$
 - $\lim_{x \rightarrow 1^+} f(x) = 5$
 - f has irremovable discontinuity at $x=1$
5. If $f(x) = 3x^{10} - 7x^8 + 5x^6 - 21x^3 + 3x^2 - 7$ then the value of $\lim_{x \rightarrow 1^+} \frac{f(1-h) - f(1)}{h^3 + 3h}$ is
- $-\frac{53}{3}$
 - $-\frac{22}{3}$
 - $\frac{53}{3}$
 - $\frac{22}{3}$
6. If the triangle formed by the lines $x^2 - y^2 = 0$ and the line $lx + 2y = 1$ is isosceles then $l =$
- 1
 - 2
 - 3
 - 0
7. Using L'Hospital's rule or otherwise evaluate the limit $\lim_{x \rightarrow 0} \frac{(e^{2x^2} - 1 - 2x^2)(\cos x - 1)}{(\sin 3x - \ln(1 + 3x))x^4}$
8. Evaluate $\lim_{x \rightarrow 0} \frac{e^x - \ln(x + e)}{e^x - 1}$ Use of L'Hospital's rule or surd expansion not allowed.
9. Find all real numbers t satisfying the equation $(3^t - 9)^3 + (9^t - 3)^3 = (9^t + 3^t - 12)^3$
10. Find $g'(3)$ if $g(x) = x \cdot 2^{u(x)}$ where $h(3) = -2$ and $h'(3) = 5$