

1. If $\tan A$ and $\tan B$ are the roots of the equation $x^2 - ax + b = 0$ then the value of $\sin^2(A + B)$ is
- $\frac{a^2}{a^2 + (1-b)^2}$
 - $\frac{a^2}{a^2 + b^2}$
 - $\frac{a^2}{(b+a)^2}$
 - $\frac{a^2}{b^2(1-a)^2}$
2. If a, b, c are distinct positive reals in G.P then $\log_a n, \log_b n, \log_c n (n > 0, n \neq 1)$ are in
- A.P
 - G.P
 - H.P
 - none of these
3. If $A = 340^\circ$ then $2\sin \frac{A}{2}$ is identical to
- $\sqrt{1 + \sin A} + \sqrt{1 - \sin A}$
 - $-\sqrt{1 + \sin A} - \sqrt{1 - \sin A}$
 - $\sqrt{1 + \sin A} - \sqrt{1 - \sin A}$
 - $-\sqrt{1 + \sin A} + \sqrt{1 - \sin A}$
4. The value of $(0.2)^{\log_{\sqrt{5}}(1/4 + 1/8 + 1/16 + \dots + \infty)}$ is equal to
- 4
 - 6
 - 8
 - 2
5. The set of angles between 0 and 2π satisfying equation $4\cos^2\theta - 2\sqrt{2}\cos\theta - 1 = 0$ is
- $\left\{ \frac{\pi}{12}, \frac{5\pi}{12}, \frac{19\pi}{12}, \frac{23\pi}{12} \right\}$
 - $\left\{ \frac{\pi}{12}, \frac{7\pi}{12}, \frac{19\pi}{12}, \frac{23\pi}{12} \right\}$
 - $\left\{ \frac{5\pi}{12}, \frac{13\pi}{12}, \frac{19\pi}{12} \right\}$
 - $\left\{ \frac{\pi}{12}, \frac{7\pi}{12}, \frac{17\pi}{12}, \frac{23\pi}{12} \right\}$
6. Let $x = \frac{1}{1.4} + \frac{1}{4.7} + \frac{1}{7.10} + \dots + \infty$ and $y = \frac{1}{1.2} + \frac{1}{2.3} + \frac{1}{3.4} + \dots + \infty$ then
- $y = 3x$
 - $y = 2x$
 - $x + y = 1$
 - $x + y = 3/2$
7. If x AM's are inserted between x^2 and 1 then the value of the x^{th} arithmetic mean is
- $1 - x$
 - $1 + x$
 - $x^2 - x + 1$
 - x
8. A regular hexagon and a regular dodecagon are inscribed in the same circle. If the side of the dodecagon is $(\sqrt{3} - 1)$, then the side of the hexagon is
- 1
 - 2

- (c) $\sqrt{2}$
 (d) $2\sqrt{2}$
9. If $3 + \frac{1}{4}(3+d) + \frac{1}{4^2}(3+2d) + \dots + \text{upto } \infty = 8$ then the value of d is
 (a) 9
 (b) 5
 (c) 1
 (d) none of these
10. If in a ΔABC , $\sin^3 A + \sin^3 B + \sin^3 C = 3\sin A \cdot \sin B \cdot \sin C$ then
 (a) ΔABC may be a scalene triangle
 (b) ΔABC is a right angled
 (c) ΔABC is an obtuse angled triangle
 (d) ΔABC is an equilateral triangle
11. If $a\cos^3 \alpha + 3a\cos \alpha \sin^2 \alpha = m$ and $a\sin^3 \alpha + 3a\cos^2 \alpha \sin \alpha = n$ Then $(m+n)^{2/3} + (m-n)^{2/3}$ is equal to
 (a) $2a^2$
 (b) $2a^{1/3}$
 (c) $2a^{2/3}$
 (d) $2a^3$
12. Consider the A.P $a_1, a_2, \dots, a_n, \dots$; the G.P $b_1, b_2, \dots, b_n, \dots$ such that $a_1 = b_1 = 1$; $a_9 = b_9$ and $\sum_{r=1}^9 a_r = 369$ then
 (a) $b_6 = 27$
 (b) $b_7 = 27$
 (c) $b_8 = 81$
 (d) $b_9 = 18$
13. If $\cos \alpha = \frac{2\cos \beta - 1}{2 - \cos \beta}$ then $\tan \frac{\alpha}{2} \cot \frac{\beta}{2}$ has the value equal to , where $(0 < \alpha < \pi)$ and $0 < \beta < \pi$
 (a) 2
 (b) $\sqrt{2}$
 (c) 3
 (d) $\sqrt{3}$
14. $2^{1/4}, 4^{1/8}, 8^{1/16}, 16^{1/32}, 32^{1/64}, \dots, \infty$ is equal to
 (a) 2
 (b) 1
 (c) $1/2$
 (d) $1/4$
15. If $x\sin \theta = y\sin(\theta + \frac{2\pi}{3}) = z\sin(\theta + \frac{4\pi}{3})$ then
 (a) $x+y+z=0$
 (b) $xy+yz+zx=0$
 (c) $xyz+x+y+z=1$
 (d) none
16. Consider a decreasing G.P $g_1, g_2, g_3 \dots g_n \dots$ such that $g_1 + g_2 + g_3 = 13$ and $g_1^2 + g_2^2 + g_3^2 = 91$ then which of the following does not holds ?
 (a) the greatest term of the G.P is 9
 (b) $3g_4 = g_3$
 (c) $g_1 = 1$
 (d) $g_2 = 3$

17. Number of roots of the equation $\cos^2 x + \frac{\sqrt{3}+1}{2} \sin x - \frac{\sqrt{3}}{4} - 1 = 0$ which lie in the interval $[-\pi, \pi]$ is
- 2
 - 4
 - 6
 - 8
18. The sum of the first three terms in an increasing G.P is 21 and the sum of their squares is 189. then the sum of its first n terms is
- $3(2^n - 1)$
 - $12(1 - \frac{1}{2^n})$
 - $6(1 - \frac{1}{2^n})$
 - $6(2^n - 1)$
19. If $\sin(\theta + \alpha) = a$ and $\sin(\theta + \beta) = b$ ($0 < \alpha, \beta, \theta < \frac{\pi}{2}$) then $\cos 2(\alpha - \beta) - 4ab \cos(\alpha - \beta) =$
- $1 - a^2 - b^2$
 - $1 - 2a^2 - 2b^2$
 - $2 + a^2 + b^2$
 - $2 - a^2 - b^2$
20. If $S_n = \frac{1}{1^3} + \frac{1+2}{1^3+2^3} + \dots + \frac{1+2+3+\dots+n}{1^3+2^3+3^3+\dots+n^3}$, $n = 1, 2, 3, \dots$. Then S_n is not greater than
- 1/2
 - 1
 - 2
 - 4
21. The exact value of $\cos^2 73^\circ + \cos^2 47^\circ + (\cos 73^\circ \cdot \cos 47^\circ)$ is
- 1/4
 - 1/2
 - 3/4
 - 1
22. Let S_1, S_2, S_3 be the sums of the first n, 2n, 3n terms of an A.P respectively. If $S_3 = C(S_2 - S_1)$ then, C is equal to
- 4
 - 3
 - 2
 - 1
23. Maximum value of the expression $\cos \theta \cdot \sin(\theta - \frac{\pi}{6}) \forall \theta \in R$ is
- 1/2
 - $\frac{\sqrt{3}}{4}$
 - 1/4
 - 1
24. The value of the expression $(\sin x + \operatorname{cosec} x)^2 + (\cos x + \sec x)^2 - (\tan x - \cot x)^2$ wherever defined is equal to
- 0
 - 5
 - 7
 - 9
25. The roots of the equation $2 + \cot x = \operatorname{cosec} x$ always lie in the quadrant number
- I only
 - I and II
 - II and IV
 - II only